

Implication of Criterion 1

(Energy)

$$\Delta E_{CV} = 0,$$

From Energy Conservation;

$$\frac{dE_{CV}}{dt} = \dot{Q} - \dot{W} + \sum_{in} \dot{m}(h + ke + pe) - \sum_{out} \dot{m}(h + ke + pe)$$

↙
↘
→ = 0

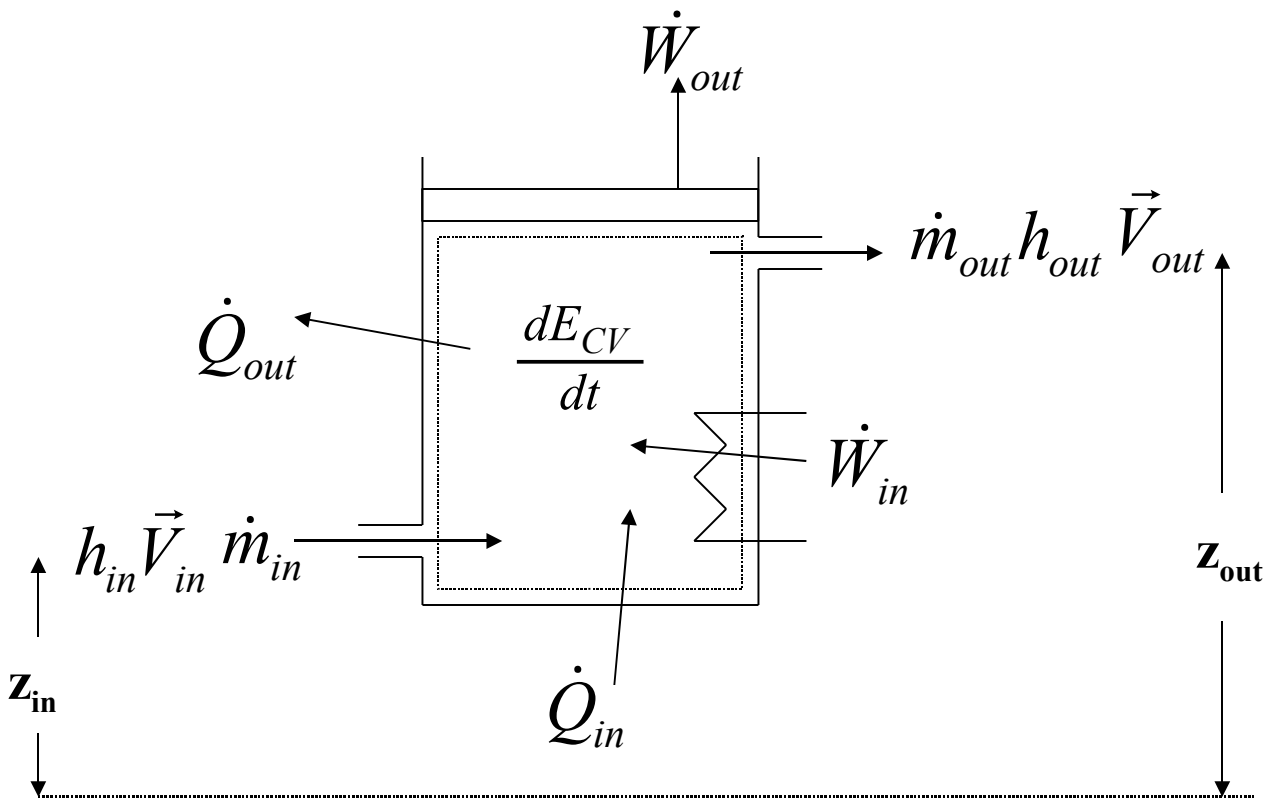
Rearrange to get Steady Flow Energy Equation

(SSSF)

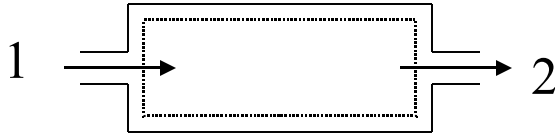
$$\dot{Q} - \dot{W} = \sum_{out} \dot{m}(h + ke + pe) - \sum_{in} \dot{m}(h + ke + pe)$$

SSSF

$$\dot{Q} - \dot{W} = \sum_{out} \underbrace{\dot{m} \left(h + \frac{\vec{V}^2}{2} + gz \right)}_{\substack{\text{For each } \mathbf{exit} \\ \text{channel}}} - \sum_{in} \underbrace{\dot{m} \left(h + \frac{\vec{V}^2}{2} + gz \right)}_{\substack{\text{For each } \mathbf{inlet} \\ \text{channel}}}$$



SSSF energy equation for 1 inlet / 1 exit



Mass

$$\dot{m}_{in} = \dot{m}_{out} \quad \text{or} \quad \dot{m}_1 = \dot{m}_2$$

Energy

$$\dot{Q} - \dot{W} = \dot{m}_2 \left(h_2 + \frac{\vec{V}_2^2}{2} + gz_2 \right) - \dot{m}_1 \left(h_1 + \frac{\vec{V}_1^2}{2} + gz_1 \right)$$

$$\dot{m}_1 = \dot{m}_2 = \dot{m}$$

$$\dot{Q} - \dot{W} = \dot{m} \left[(h_2 - h_1) + \left(\frac{\vec{V}_2^2 - \vec{V}_1^2}{2} \right) + g(z_2 - z_1) \right]$$

$$\frac{\dot{Q}}{\dot{m}} - \frac{\dot{W}}{\dot{m}} = (h_2 - h_1) + \left(\frac{\vec{V}_2^2 - \vec{V}_1^2}{2} \right) + g(z_2 - z_1)$$

$$q - w = \Delta h + \Delta ke + \Delta pe \quad (1 \text{ inlet} / 1 \text{ exit})$$

$$(\Delta = \text{exit} - \text{inlet})$$

SSSF energy equation for multiple channels but neglecting Δke , Δpe

$$\dot{Q} - \dot{W} = \sum \dot{m}_{out} h_{out} - \sum \dot{m}_{in} h_{in}$$

$$\sum \dot{m}_{in} = \sum \dot{m}_{out}$$